

CSCI 5333 DBMS
Fall 2021
Homework #8

Normalization Theory

(1) Use Armstrong's axioms and rules to prove that

$$F = \{B \rightarrow A, AC \rightarrow D, CD \rightarrow F, F \rightarrow E\}$$

implies $BC \rightarrow E$

(2) Consider $R(A, B, C, D, E)$ with

$$F = \{A \rightarrow B, BC \rightarrow DE, AB \rightarrow E, DE \rightarrow C, AE \rightarrow CD\}$$

(a) What are A^+ , B^+ , C^+ , D^+ and E^+ ?

(b) What are the candidate keys? Why?

(c) Show all prime attributes and non-prime attributes?

(d) Give a canonical cover of F ?

(e) What is the highest normal form (up to BCNF) of R ? Why?

(f) If R is not in BCNF, can you provide a lossless FD preserving decompositions of R into BCNF relations?

(3) Consider $R(A, B, C, D, E, F)$ with

$$F = \{CD \rightarrow B, BC \rightarrow D, D \rightarrow A, F \rightarrow DE, FDE \rightarrow AC, B \rightarrow F\}$$

(a) What are A^+ , B^+ , C^+ , D^+ , E^+ , F^+ ?

(b) What are the candidate keys? Why?

(c) Show all prime attributes and non-prime attributes?

(d) Give a canonical cover of F ?

(e) What is the highest normal form (up to BCNF) of R ? Why?

(f) If R is not in BCNF, can you provide a lossless FD preserving decompositions of R into BCNF relations?

(4) What are the highest normal forms of the following relations (assume they are at least in 1NF).

(a) $R(A,B,C,D)$ $\{A \rightarrow C\}$

(b) $R(A,B,C,D)$ $\{A \rightarrow B, B \rightarrow A, A \rightarrow C, C \rightarrow D, D \rightarrow AB\}$

(c) $R(A,B,C,D,E)$ $\{AB \rightarrow CD, C \rightarrow ABE\}$

(d) $R(A,B,C,D,E)$ $\{ABC \rightarrow D, E \rightarrow D\}$

(e) $R(A,B,C,D,E)$ $\{ABC \rightarrow D, D \rightarrow E\}$

(f) $R(A,B,C,D,E)$ $\{ABCE \rightarrow D, D \rightarrow BE\}$

(5) Given $R(A,B,C,D,E)$ $\{AB \rightarrow C, A \rightarrow D, BE \rightarrow A, AD \rightarrow CE\}$

It is decomposed into $R_1(A,B,C)$, $R_2(A,C,D,E)$ and $R_3(A,B,E)$.

Is the decomposition lossy? Prove your assertion.

(6) Short questions

(a) It is known that $R(A,B,C,D,E)$ has exactly two candidate keys. What are the maximum and minimum number of superkeys R may have?

(b) A relation R is in 3NF and is known to have exactly one candidate key. Can we deduce that R is also in BCNF? Prove your assertion.

(c) If the relation $R(A,B,C,D,E)$ has *exactly* five superkeys. Can you deduce how many candidate keys R have? Why?

As usual, submit your homework through Blackboard using the file name <<Yourname>>_<<YourStudentNumber>>_h8.docx.